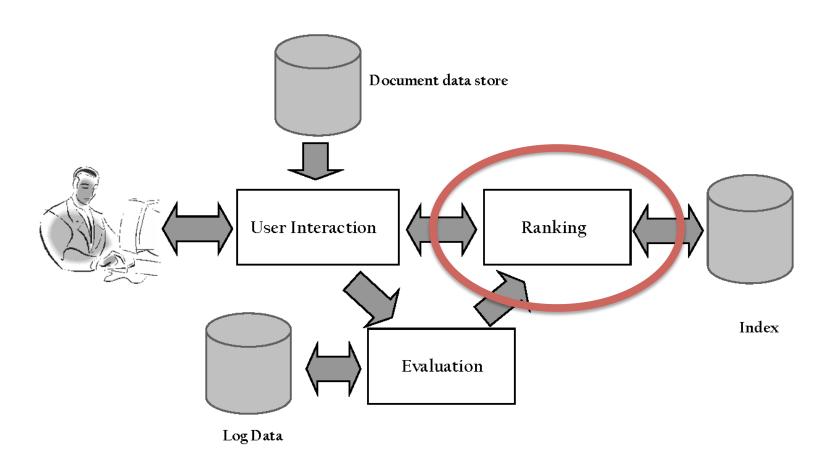
# CS6200 Information Retrieval

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# **Query Process**



### Retrieval Models

- Provide a mathematical framework for defining the search process
  - includes explanation of assumptions
  - basis of many ranking algorithms
  - can be implicit
    - Retrieval model developed by trial and error
- Progress in retrieval models has corresponded with improvements in effectiveness
- Theories about—i.e., models of—relevance

#### Relevance

- Complex concept that has been studied for some time
  - Many factors to consider
  - People often disagree when making relevance judgments
- Retrieval models make various assumptions about relevance to simplify problem
  - e.g., topical vs. user relevance
  - e.g., binary vs. multi-valued relevance

## Topical vs. User Relevance

- Topical Relevance
  - Document and query are on the same topic
  - Query: "U.S. Presidents"
  - Document: Wikipedia article on Abraham Lincoln
- User Relevance
  - Incorporate factors beside document topic
    - Document freshness
    - Style
    - Content presentation

# Binary vs. Multi-Valued Relevance

- Binary Relevance
  - The document is either relevant or not

- Multi-Valued Relevance
  - Makes the evaluation task easier for the judges
  - Not as important for retrieval models
  - Many retrieval models calculate the probability of relevance

### Retrieval Model Overview

- Older models
  - Boolean retrieval
  - Vector Space model
- Probabilistic Models
  - BM25
  - Language models
- Combining evidence
  - Inference networks
  - Learning to Rank

#### **Boolean Retrieval**

- Two possible outcomes for query processing
  - TRUE and FALSE
  - "exact-match" retrieval; "set" retrieval
  - simplest form of ranking
- Query usually specified using Boolean operators
  - AND, OR, NOT
  - proximity operators and wildcards also used

### **Boolean Retrieval**

#### Advantages

- Results are predictable, relatively easy to explain
- Many different features can be incorporated
- Efficient processing since many documents can be eliminated from search

#### Disadvantages

- Effectiveness depends entirely on user
- Simple queries usually don't work well
- Complex queries are difficult

# Searching by Numbers

- Sequence of queries driven by number of retrieved documents
  - 1. lincoln
  - 2. president AND lincoln
  - president AND lincoln AND NOT (automobile OR car)
  - president AND lincoln AND biography AND life AND birthplace AND gettysburg AND NOT (automobile OR car)
  - president AND lincoln AND (biography OR life OR birthplace OR gettysburg) AND NOT (automobile OR car)

- Documents and query represented by a vector of term weights
- Collection represented by a matrix of term weights

```
D_{i} = (d_{i1}, d_{i2}, \dots, d_{it}) \qquad Q = (q_{1}, q_{2}, \dots, q_{t})
Term_{1} \quad Term_{2} \quad \dots \quad Term_{t}
Doc_{1} \quad d_{11} \quad d_{12} \quad \dots \quad d_{1t}
Doc_{2} \quad d_{21} \quad d_{22} \quad \dots \quad d_{2t}
\vdots \qquad \vdots
Doc_{n} \quad d_{n1} \quad d_{n2} \quad \dots \quad d_{nt}
```

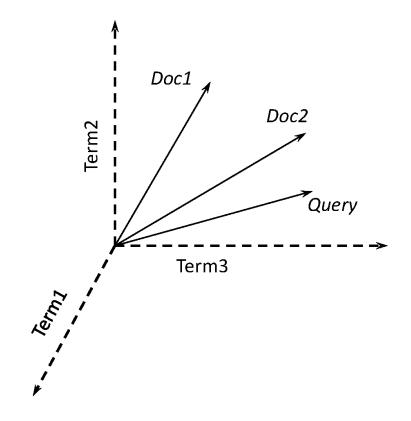
- D<sub>1</sub> Tropical Freshwater Aquarium Fish.
- D<sub>2</sub> Tropical Fish, Aquarium Care, Tank Setup.
- D<sub>3</sub> Keeping Tropical Fish and Goldfish in Aquariums, and Fish Bowls.
- D<sub>4</sub> The Tropical Tank Homepage Tropical Fish and Aquariums.

Terms	Documen			
	$D_1$	$D_2$	$D_3$	$D_4$
aquarium	1	1	1	1
bowl	0	0	1	0
care	0	1	0	0
fish	1	1	2	1
freshwater	1	0	0	0
goldfish	0	0	1	0
homepage	0	0	0	1
keep	0	0	1	0
setup	0	1	0	0
tank	0	1	0	1
tropical	1	1	1	2

Query: "tropical fish"

Term	Query
aquarium	0
bowl	0
care	0
fish	1
freshwater	0
goldfish	0
homepage	0
keep	0
setup	0
tank	0
tropical	1

 3-d pictures useful, but can be misleading for high-dimensional space



- Documents ranked by distance between points representing query and documents
  - Similarity measure more common than a distance or dissimilarity measure
  - e.g. Cosine correlation

$$Cosine(D_{i}, Q) = \frac{\sum_{j=1}^{t} d_{ij} \cdot q_{j}}{\sqrt{\sum_{j=1}^{t} d_{ij}^{2} \cdot \sum_{j=1}^{t} q_{j}^{2}}}$$

# Similarity Calculation

- Consider two documents  $D_{1}$ ,  $D_{2}$  and a query Q
  - $D_1 = (0.5, 0.8, 0.3), D_2 = (0.9, 0.4, 0.2), Q = (1.5, 1.0, 0)$

Cosine(D<sub>1</sub>, Q) = 
$$\frac{(0.5 \times 1.5) + (0.8 \times 1.0)}{\sqrt{(0.5^2 + 0.8^2 + 0.3^2)(1.5^2 + 1.0^2)}}$$
$$= \frac{1.55}{\sqrt{(0.98 \times 3.25)}} = 0.87$$

Cosine(D<sub>2</sub>, Q) = 
$$\frac{(0.9 \times 1.5) + (0.4 \times 1.0)}{\sqrt{(0.9^2 + 0.4^2 + 0.2^2)(1.5^2 + 1.0^2)}}$$
$$= \frac{1.75}{\sqrt{(1.01 \times 3.25)}} = 0.97$$

### Difference from Boolean Retrieval

- Similarity calculation has two factors that distinguish it from Boolean retrieval
  - Number of matching terms affects similarity
  - Weight of matching terms affects similarity
- Documents can be ranked by their similarity scores

# Term Weights

- *tf.idf* weight
  - Term frequency weight measures importance in document:  $tf_{ik} = \frac{f_{ik}}{\sum f_{ij}}$
  - Inverse document frequency measures importance in collection:  $idf_k = \log \frac{N}{n_k}$
  - Heuristic combination

$$d_{ik} = \frac{(\log(f_{ik}) + 1) \cdot \log(N/n_k)}{\sqrt{\sum_{k=1}^{t} [(\log(f_{ik}) + 1.0) \cdot \log(N/n_k)]^2}}$$

#### Relevance Feedback

- Rocchio algorithm
- Optimal query
  - Maximizes the difference between the average vector representing the relevant documents and the average vector representing the non-relevant documents
- Modifies query according to

$$q'_{j} = \alpha.q_{j} + \beta.\frac{1}{|Rel|} \sum_{D_{i} \in Rel} d_{ij} - \gamma.\frac{1}{|Nonrel|} \sum_{D_{i} \in Nonrel} d_{ij}$$

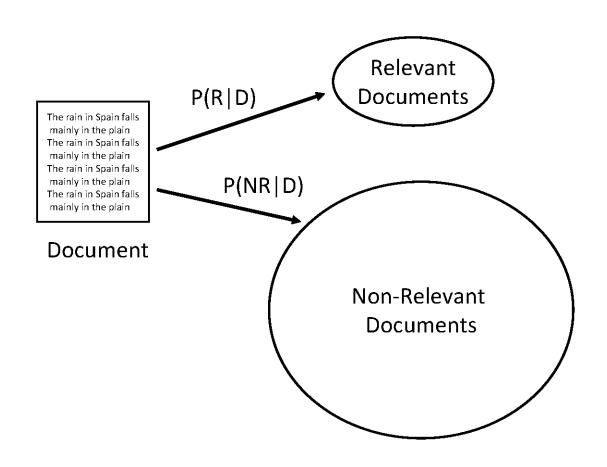
- $-\alpha$ ,  $\beta$ , and  $\gamma$  are parameters
  - Typical values 8, 16, 4

- Advantages
  - Simple computational framework for ranking
  - Any similarity measure or term weighting scheme could be used
- Disadvantages
  - Assumption of term independence
  - No predictions about techniques for effective ranking

# Probability Ranking Principle

- Robertson (1977)
  - "If a reference retrieval system's response to each request is a ranking of the documents in the collection in order of decreasing probability of relevance to the user who submitted the request,
  - where the probabilities are estimated as accurately as possible on the basis of whatever data have been made available to the system for this purpose,
  - the overall effectiveness of the system to its user will be the best that is obtainable on the basis of those data."

### IR as Classification



# **Bayes Classifier**

- Bayes Decision Rule
  - A document D is relevant if P(R|D) > P(NR|D)
- Estimating probabilities
  - use Bayes Rule

$$P(R|D) = \frac{P(D|R)P(R)}{P(D)}$$

- classify a document as relevant if

$$\frac{P(D|R)}{P(D|NR)} > \frac{P(NR)}{P(R)}$$

• This is likelihood ratio

# Estimating P(D|R)

Assume independence

$$P(D|R) = \prod_{i=1}^{t} P(d_i|R)$$

- Binary independence model
  - document represented by a vector of binary features indicating term occurrence (or nonoccurrence)
  - $-p_i$  is probability that term i occurs (i.e., has value 1) in relevant document,  $s_i$  is probability of occurrence in non-relevant document

# Binary Independence Model

$$\frac{P(D|R)}{P(D|NR)} = \prod_{i:d_i=1} \frac{p_i}{s_i} \cdot \prod_{i:d_i=0} \frac{1-p_i}{1-s_i}$$

$$= \prod_{i:d_i=1} \frac{p_i}{s_i} \cdot \left( \prod_{i:d_i=1} \frac{1-s_i}{1-p_i} \cdot \prod_{i:d_i=1} \frac{1-p_i}{1-s_i} \right) \cdot \prod_{i:d_i=0} \frac{1-p_i}{1-s_i}$$

$$= \prod_{i:d_i=1} \frac{p_i(1-s_i)}{s_i(1-p_i)} \cdot \prod_i \frac{1-p_i}{1-s_i}$$

# Binary Independence Model

Scoring function is

$$\sum_{i:d_i=1} \log \frac{p_i(1-s_i)}{s_i(1-p_i)}$$

- Query provides information about relevant documents
- If we assume  $p_i$  constant,  $s_i$  approximated by entire collection, get idf-like weight

$$\log \frac{0.5(1-\frac{n_i}{N})}{\frac{n_i}{N}(1-0.5)} = \log \frac{N-n_i}{n_i}$$

# **Contingency Table**

	Relevant	Non-relevant	Total
$d_i = 1$	$r_i$	$n_i - r_i$	$n_i$
$d_i = 0$	$R-r_i$	$N-n_i-R+r_i$	$N-r_i$
Total	R	N-R	N

$$p_i = (r_i + 0.5)/(R+1)$$
$$s_i = (n_i - r_i + 0.5)/(N - R + 1)$$

#### Gives scoring function:

$$\sum_{i:d_i=q_i=1} \log \frac{(r_i+0.5)/(R-r_i+0.5)}{(n_i-r_i+0.5)/(N-n_i-R+r_i+0.5)}$$

#### **BM25**

- Popular and effective ranking algorithm based on binary independence model
  - adds document and query term weights

$$\sum_{i \in Q} \log \frac{(r_i + 0.5)/(R - r_i + 0.5)}{(n_i - r_i + 0.5)/(N - n_i - R + r_i + 0.5)} \cdot \frac{(k_1 + 1)f_i}{K + f_i} \cdot \frac{(k_2 + 1)qf_i}{k_2 + qf_i}$$

- $-k_1$ ,  $k_2$  and K are parameters whose values are set empirically
- $-K = k_1((1-b) + b \cdot \frac{dl}{avdl})$  dl is doc length
- Typical TREC value for  $k_1$  is 1.2,  $k_2$  varies from 0 to 1000, b = 0.75

### BM25 Example

- Query with two terms, "president lincoln", (qf = 1)
- No relevance information (r and R are zero)
- N = 500,000 documents
- "president" occurs in 40,000 documents  $(n_1 = 40,000)$
- "lincoln" occurs in 300 documents ( $n_2 = 300$ )
- "president" occurs 15 times in doc  $(f_1 = 15)$
- "lincoln" occurs 25 times  $(f_2 = 25)$
- document length is 90% of the average length (dl/avdl = .9)
- $k_1 = 1.2$ , b = 0.75, and  $k_2 = 100$
- $K = 1.2 \cdot (0.25 + 0.75 \cdot 0.9) = 1.11$

### BM25 Example

$$BM25(Q,D) =$$

$$\log \frac{(0+0.5)/(0-0+0.5)}{(40000-0+0.5)/(500000-40000-0+0+0.5)} \times \frac{(1.2+1)15}{1.11+15} \times \frac{(100+1)1}{100+1} + \log \frac{(0+0.5)/(0-0+0.5)}{(300-0+0.5)/(500000-300-0+0+0.5)} \times \frac{(1.2+1)25}{1.11+25} \times \frac{(100+1)1}{100+1}$$

$$= \log 460000.5/40000.5 \cdot 33/16.11 \cdot 101/101$$

$$+ \log 499700.5/300.5 \cdot 55/26.11 \cdot 101/101$$

$$= 2.44 \cdot 2.05 \cdot 1 + 7.42 \cdot 2.11 \cdot 1$$

$$= 5.00 + 15.66 = 20.66$$

## BM25 Example

#### Effect of term frequencies

Frequency of	Frequency of	$\overline{\mathrm{BM25}}$
"president"	"lincoln"	score
15	25	20.66
15	1	12.74
15	0	5.00
1	25	18.2
0	25	15.66

### Language Model

- Language model
  - Probability distribution over strings of text
- Unigram language model
  - generation of text consists of pulling words out of a "bucket" according to the probability distribution and replacing them
- N-gram language model
  - some applications use bigram and trigram language models where probabilities depend on previous words

### Language Model

- A topic in a document or query can be represented as a language model
  - i.e., words that tend to occur often when discussing a topic will have high probabilities in the corresponding language model
- Multinomial distribution over words
  - text is modeled as a finite sequence of words,
     where there are t possible words at each point in the sequence
  - commonly used, but not only possibility
  - doesn't model burstiness

### LMs for Retrieval

- 3 possibilities:
  - probability of generating the query text from a document language model
  - probability of generating the document text from a query language model
  - comparing the language models representing the query and document topics
- Models of topical relevance

# Query-Likelihood Model

- Rank documents by the probability that the query could be generated by the document model (i.e. same topic)
- Given query, start with P(D|Q)
- Using Bayes' Rule

$$p(D|Q) \stackrel{rank}{=} P(Q|D)P(D)$$

Assuming prior is uniform, unigram model

$$P(Q|D) = \prod_{i=1}^{n} P(q_i|D)$$

## **Estimating Probabilities**

Obvious estimate for unigram probabilities is

$$P(q_i|D) = \frac{f_{q_i,D}}{|D|}$$

- Maximum likelihood estimate
  - makes the observed value of  $f_{q,D}$  most likely
- If query words are missing from document, score will be zero
  - Missing 1 out of 4 query words same as missing 3 out of 4

#### Smoothing

- Document texts are a sample from the language model
  - Missing words should not have zero probability of occurring
- Smoothing is a technique for estimating probabilities for missing (or unseen) words
  - lower (or discount) the probability estimates for words that are seen in the document text
  - assign that "left-over" probability to the estimates for the words that are not seen in the text
  - What does this do to the likelihood of the document?

#### **Estimating Probabilities**

- Estimate for unseen words is  $\alpha_D P(q_i | C)$ 
  - $-P(q_i|C)$  is the probability for query word i in the collection language model for collection C (background probability)
  - $-\alpha_D$  is a parameter
- Estimate for words that occur is

$$(1 - \alpha_D) P(q_i | D) + \alpha_D P(q_i | C)$$

• Different forms of estimation come from different  $\alpha_D$ 

### Jelinek-Mercer Smoothing

- $\alpha_D$  is a constant,  $\lambda$
- Gives estimate of

$$p(q_i|D) = (1 - \lambda) \frac{f_{q_i,D}}{|D|} + \lambda \frac{c_{q_i}}{|C|}$$

Ranking score

$$P(Q|D) = \prod_{i=1}^{n} ((1-\lambda) \frac{f_{q_i,D}}{|D|} + \lambda \frac{c_{q_i}}{|C|})$$

- Use logs for convenience
  - accuracy problems multiplying small numbers

$$\log P(Q|D) = \sum_{i=1}^{n} \log((1-\lambda)\frac{f_{q_i,D}}{|D|} + \lambda \frac{c_{q_i}}{|C|})$$

# Where is *tf.idf* Weight?

$$\log P(Q|D) = \sum_{i=1}^{n} \log((1-\lambda)\frac{f_{q_{i},D}}{|D|} + \lambda \frac{c_{q_{i}}}{|C|})$$

$$= \sum_{i:f_{q_{i},D}>0} \log((1-\lambda)\frac{f_{q_{i},D}}{|D|} + \lambda \frac{c_{q_{i}}}{|C|}) + \sum_{i:f_{q_{i},D}=0} \log(\lambda \frac{c_{q_{i}}}{|C|})$$

$$= \sum_{i: f_{q_{i},D} > 0} \log \frac{\left((1-\lambda)\frac{f_{q_{i},D}}{|D|} + \lambda\frac{c_{q_{i}}}{|C|}\right)}{\lambda\frac{c_{q_{i}}}{|C|}} + \sum_{i=1}^{n} \log(\lambda\frac{c_{q_{i}}}{|C|})$$

$$\stackrel{rank}{=} \sum_{i: f_{q_{i},D} > 0} \log \left(\frac{\left((1-\lambda)\frac{f_{q_{i},D}}{|D|}}{\lambda\frac{c_{q_{i}}}{|C|}} + 1\right)\right)$$

proportional to the term frequency, inversely proportional to the collection frequency

### **Dirichlet Smoothing**

•  $\alpha_D$  depends on document length

$$\alpha_D = \frac{\mu}{|D| + \mu}$$

Gives probability estimation of

$$p(q_i|D) = \frac{f_{q_i,D} + \mu \frac{c_{q_i}}{|D| + \mu}}{|D| + \mu}$$

and document score

$$\log P(Q|D) = \sum_{i=1}^{n} \log \frac{f_{q_i,D} + \mu \frac{\partial q_i}{|C|}}{|D| + \mu}$$

### Query Likelihood Example

For the term "president"

$$-f_{qi,D}$$
 = 15,  $c_{qi}$  = 160,000

For the term "lincoln"

$$-f_{qi,D}$$
 = 25,  $c_{qi}$  = 2,400

- number of word occurrences in the document |
   d | is assumed to be 1,800
- number of word occurrences in the collection is
   10<sup>9</sup>
  - 500,000 documents times an average of 2,000 words
- $\mu = 2,000$

## Query Likelihood Example

$$QL(Q, D) = \log \frac{15 + 2000 \times (1.6 \times 10^{5}/10^{9})}{1800 + 2000} + \log \frac{25 + 2000 \times (2400/10^{9})}{1800 + 2000}$$
$$= \log(15.32/3800) + \log(25.005/3800)$$
$$= -5.51 + -5.02 = -10.53$$

 Negative number because summing logs of small numbers

# Query Likelihood Example

Frequency of	Frequency of	QL
"president"	"lincoln"	score
15	25	-10.53
15	1	-13.75
15	0	-19.05
1	25	-12.99
0	25	-14.40

#### Relevance Models

- Relevance model language model representing information need
  - query and relevant documents are samples from this model
- P(D/R) probability of generating the text in a document given a relevance model
  - document likelihood model
  - less effective than query likelihood due to difficulties comparing across documents of different lengths

#### Pseudo-Relevance Feedback

- Estimate relevance model from query and top-ranked documents
- Rank documents by similarity of document model to relevance model
- Kullback-Leibler divergence (KL-divergence) is a well-known measure of the difference between two probability distributions

#### **KL-Divergence**

 Given the true probability distribution P and another distribution Q that is an approximation to P,

$$KL(P||Q) = \sum_{x} P(x) \log \frac{P(x)}{Q(x)}$$

 Use negative KL-divergence for ranking, and assume relevance model R is the true distribution (not symmetric),

$$\sum_{w \in V} P(w|R) \log P(w|D) - \sum_{w \in V} P(w|R) \log P(w|R)$$

#### **KL-Divergence**

 Given a simple maximum likelihood estimate for P(w/R), based on the frequency in the query text, ranking score is

$$\sum_{w \in V} \frac{f_{w,Q}}{|Q|} \log P(w|D)$$

- rank-equivalent to query likelihood score
- Query likelihood model is a special case of retrieval based on relevance model

# Estimating the Relevance Model

 Probability of pulling a word w out of the "bucket" representing the relevance model depends on the n query words we have just pulled out

$$P(w|R) \approx P(w|q_1 \dots q_n)$$

By definition

$$P(w|R) \approx \frac{P(w,q_1...q_n)}{P(q_1...q_n)}$$

#### Estimating the Relevance Model

Joint probability is

$$P(w, q_1 \dots q_n) = \sum_{D \in \mathcal{C}} p(D) P(w, q_1 \dots q_n | D)$$

Assume

$$P(w, q_1 \dots q_n | D) = P(w | D) \prod_{i=1}^n P(q_i | D)$$

Gives

$$P(w, q_1 \dots q_n) = \sum_{D \in \mathcal{C}} P(D) P(w|D) \prod_{i=1}^n P(q_i|D)$$

#### Estimating the Relevance Model

- P(D) usually assumed to be uniform
- P(w, q1...qn) is simply a weighted average of the language model probabilities for w in a set of documents, where the weights are the query likelihood scores for those documents
- Formal model for pseudo-relevance feedback
  - query expansion technique

#### Pseudo-Feedback Algorithm

- 1. Rank documents using the query likelihood score for query Q.
- 2. Select some number of the top-ranked documents to be the set  $\mathcal{C}$ .
- 3. Calculate the relevance model probabilities P(w|R).  $P(q_1 \ldots q_n)$  is used as a normalizing constant and is calculated as

$$P(q_1 \dots q_n) = \sum_{w \in V} P(w, q_1 \dots q_n)$$

4. Rank documents again using the KL-divergence score

$$\sum_{w} P(w|R) \log P(w|D)$$

# Example from Top 10 Docs

president lincoln	abraham lincoln	fishing	$tropical\ fish$
lincoln	lincoln	fish	fish
president	america	$\operatorname{farm}$	$\operatorname{tropic}$
room	president	salmon	japan
bedroom	faith	new	aquarium
house	guest	wild	water
white	abraham	water	species
america	new	$\operatorname{caught}$	aquatic
guest	room	$\operatorname{catch}$	fair
serve	christian	$\operatorname{tag}$	china
bed	history	$\operatorname{time}$	$\operatorname{coral}$
washington	public	eat	source
old	bedroom	raise	$\operatorname{tank}$
office	war	$\operatorname{city}$	$\operatorname{reef}$
war	politics	people	animal
long	old	fishermen	tarpon
abraham	national	boat	fishery

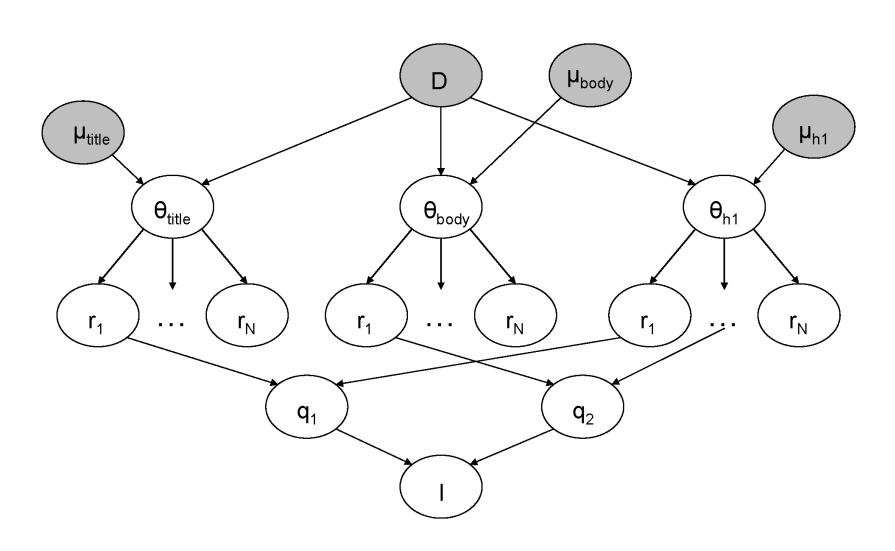
# Example from Top 50 Docs

president lincoln	abraham lincoln	fishing	$tropical\ fish$
lincoln	lincoln	fish	fish
president	president	water	$\operatorname{tropic}$
america	america	$\operatorname{catch}$	water
new	abraham	$\operatorname{reef}$	$\operatorname{storm}$
national	war	fishermen	species
great	man	river	boat
white	civil	new	sea
war	new	year	river
washington	history	$\operatorname{time}$	$\operatorname{country}$
clinton	two	bass	tuna
house	room	boat	world
history	booth	world	$\operatorname{million}$
$\operatorname{time}$	time	$\operatorname{farm}$	state
center	politics	angle	$\operatorname{time}$
kennedy	public	fly	japan
room	guest	trout	$\operatorname{mile}$

#### **Combining Evidence**

- Effective retrieval requires the combination of many pieces of evidence about a document's potential relevance
  - have focused on simple word-based evidence
  - many other types of evidence
    - structure, PageRank, metadata, even scores from different models
- Inference network model is one approach to combining evidence
  - uses Bayesian network formalism

#### Inference Network



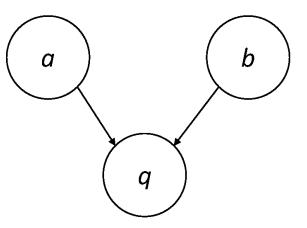
#### Inference Network

- *Document node* (D) corresponds to the event that a document is observed
- Representation nodes (r<sub>i</sub>) are document features (evidence)
  - Probabilities associated with those features are based on language models  $\theta$  estimated using the parameters  $\mu$
  - one language model for each significant document structure
  - r<sub>i</sub> nodes can represent proximity features, or other types of evidence (e.g. date)

#### Inference Network

- Query nodes (q<sub>i</sub>) are used to combine evidence from representation nodes and other query nodes
  - represent the occurrence of more complex evidence and document features
  - a number of combination operators are available
- Information need node (I) is a special query node that combines all of the evidence from the other query nodes
  - network computes  $P(I|D, \mu)$

# **Example: AND Combination**



a and b are parent nodes for g

P(q = TRUE a, b)	a	b
0	FALSE	FALSE
0	FALSE	TRUE
0	TRUE	FALSE
1	TRUE	TRUE

#### **Example: AND Combination**

- Combination must consider all possible states of parents
- Some combinations can be computed efficiently

```
\begin{aligned} bel_{and}(q) &= p_{00}P(a = \mathsf{FALSE})P(b = \mathsf{FALSE}) \\ &+ p_{01}P(a = \mathsf{FALSE})P(b = \mathsf{TRUE}) \\ &+ p_{10}P(a = \mathsf{TRUE})P(b = \mathsf{FALSE}) \\ &+ p_{11}P(a = \mathsf{TRUE})P(b = \mathsf{TRUE}) \\ &= 0 \cdot (1-p_a)(1-p_b) + 0 \cdot (1-p_a)p_b + 0 \cdot p_a(1-p_b) + 1 \cdot p_a p_b \\ &= p_a p_b \end{aligned}
```

# Inference Network Operators

$$bel_{not}(q) = 1 - p_1$$

$$bel_{or}(q) = 1 - \prod_{i}^{n} (1 - p_i)$$

$$bel_{and}(q) = \prod_{i}^{n} p_i$$

$$bel_{wand}(q) = \prod_{i}^{n} p_i^{wt_i}$$

$$bel_{max}(q) = max\{p_1, p_2, \dots, p_n\}$$

$$bel_{sum}(q) = \frac{\sum_{i}^{n} p_i}{n}$$

$$bel_{wsum}(q) = \frac{\sum_{i}^{n} wt_i p_i}{\sum_{i}^{n} wt_i}$$

- A document is viewed as a sequence of text that may contain arbitrary tags
- A single context is generated for each unique tag name
- An extent is a sequence of text that appears within a single begin/end tag pair of the same type as the context

```
title context:
<html>
                                                         <title>Department Descriptions</title>
<head>
<title>Department Descriptions</title>
                                                      h1 context:
</head>
                                                         <h l>Agriculture</h l>
<body>
                                                         <hl>>Chemistry</hl> ...
The following list describes ...
                                                         <h1>Computer Science</h1> ...
<h1>Agriculture</h1> ...
                                                         <h1>Electrical Engineering</h1> ...
<h1>Chemistry</h1> ...
<h1>Computer Science</h1> ...
                                                      body context:
<h1>Electrical Engineering</h1> ...
                                                         <body> The following list describes ...
</body>
                                                         <h I > Agriculture </h I > ...
</html>
                                                         <h1>Chemistry</h1> ...
                                                         <h1>Computer Science</h1> ...
                                                         <h1>Electrical Engineering</h1> ...
                                                         </body>
```

#### Simple terms:

```
term – term that will be normalized and stemmed. "term" – term is not normalized or stemmed. Examples: presidents "NASA"
```

#### Proximity terms:

```
#od:N( ... ) - ordered window - terms must appear ordered, with
at most N-1 terms between each.
#od( ... ) - unlimited ordered window - all terms must appear
ordered anywhere within current context.
#uw:N( ... ) - unordered window - all terms must appear within a
window of length N in any order.
#uw( ... ) - unlimited unordered window - all terms must appear
within current context in any order.
Examples:
#od:1(white house) – matches "white house" as an exact phrase.
#od:2(white house) – matches "white * house" (where * is any word
or null).
#uw:2(white house) – matches "white house" and "house white".
```

#### Synonyms:

```
#syn( ... )
#wsyn( ... )
Examples:
#syn(dog canine) - simple synonym based on two terms.
#syn( #od:1(united states) #od:1(united states of america) ) - creates a synonym from two proximity terms.
#wsyn( 1.0 donald 0.8 don 0.5 donnie ) - weighted synonym indicating relative importance of terms.
```

#### Anonymous terms:

```
#any:.() – used to match extent types Examples:
#any:person() – matches any occurrence of a person extent.
#od:1(lincoln died in #any:date()) – matches exact phrases of the form: "lincoln died in <date>...</date>".
```

#### Context restriction and evaluation:

```
expression.C1,...,CN — matches when the expression appears in all contexts C1 through CN.
```

expression.(C1,...,CN) – evaluates the expression using the language model defined by the concatenation of contexts C1...CN within the document.

#### Examples:

dog.title – matches the term "dog" appearing in a title extent.

#uw(smith jones).author – matches when the two names "smith" and "jones" appear in an author extent.

dog.(title) – evaluates the term based on the title language model for the document.

#od:1(abraham lincoln).person.(header) — builds a language model from all of the "header" text in the document and evaluates #od:1(abraham lincoln).person in that context (i.e., matches only the exact phrase appearing within a person extent within the header context).

#### Belief operators:

```
#combine(...) – this operator is a normalized version of the bel_{and}(q) operator in the inference network model. See the discussion below for more details.
```

#weight(...) – this is a normalized version of the  $bel_{wand}(q)$  operator.

#filter(...) – this operator is similar to #combine, but with the difference that the document must contain at least one instance of all terms (simple, proximity, synonym, etc.). The evaluation of nested belief operators is not changed.

#### Examples:

#combine( #syn(dog canine) training ) – rank by two terms, one of which is a synonym.

#combine( biography #syn(#od:1(president lincoln) #od:1(abraham lincoln)) ) - rank using two terms, one of which is a synonym of "president lincoln" and "abraham lincoln".

#weight( 1.0 #od:1(civil war) 3.0 lincoln 2.0 speech ) – rank using three terms, and weight the term "lincoln" as most important, followed by "speech", then "civil war".

#filter( aquarium #combine(tropical fish) ) – consider only those documents containing the word "aquarium" and "tropical" or "fish", and rank them according to the query #combine(aquarium #combine(tropical fish)).

#filter( #od:1(john smith).author) #weight( 2.0 europe 1.0 travel ) – rank documents about "europe" or "travel" that have "John Smith" in the author context.

#### Web Search

- Most important, but not only, search application
- Major differences to TREC news
  - Size of collection
  - Connections between documents
  - Range of document types
  - Importance of spam
  - Volume of queries
  - Range of query types

### Search Taxonomy

- Informational
  - Finding information about some topic which may be on one or more web pages
  - Topical search
- Navigational
  - finding a particular web page that the user has either seen before or is assumed to exist
- Transactional
  - finding a site where a task such as shopping or downloading music can be performed

### Web Search

- For effective navigational and transactional search, need to combine features that reflect user relevance
- Commercial web search engines combine evidence from *hundreds* of features to generate a ranking score for a web page
  - page content, page metadata, anchor text, links (e.g., PageRank), and user behavior (click logs)
  - page metadata e.g., "age", how often it is updated, the URL of the page, the domain name of its site, and the amount of text content

### Search Engine Optimization

- SEO: understanding the relative importance of features used in search and how they can be manipulated to obtain better search rankings for a web page
  - e.g., improve the text used in the title tag, improve the text in heading tags, make sure that the domain name and URL contain important keywords, and try to improve the anchor text and link structure
  - Some of these techniques are regarded as not appropriate by search engine companies

### Web Search

- In TREC evaluations, most effective features for navigational search are:
  - text in the title, body, and heading (h1, h2, h3, and h4) parts of the document, the anchor text of all links pointing to the document, the PageRank number, and the inlink count
- Given size of Web, many pages will contain all query terms
  - Ranking algorithm focuses on discriminating between these pages
  - Word proximity is important

### **Term Proximity**

- Many models have been developed
- N-grams are commonly used in commercial web search
- Dependence model based on inference net has been effective in TREC e.g.

## Example Web Query

```
#weight(
         0.1 #weight( 0.6 #prior(pagerank) 0.4 #prior(inlinks))
         1.0 \# weight(
             0.9 #combine(
                 #weight( 1.0 pet.(anchor) 1.0 pet.(title)
                           3.0 pet.(body) 1.0 pet.(heading))
                 #weight( 1.0 therapy.(anchor) 1.0 therapy.(title)
                           3.0 therapy.(body) 1.0 therapy.(heading)))
             0.1 \# weight(
                 1.0 #od:1(pet therapy).(anchor) 1.0 #od:1(pet therapy).(title)
                 3.0 \# od:1(pet therapy).(body) 1.0 \# od:1(pet therapy).(heading))
             0.1 \# weight(
                 1.0 \#uw:8(pet therapy).(anchor) 1.0 \#uw:8(pet therapy).(title)
                 3.0 \#uw:8(pet therapy).(body) 1.0 \#uw:8(pet therapy).(heading)))
```

## Machine Learning and IR

- Considerable interaction between these fields
  - Rocchio algorithm (60s) is a simple learning approach
  - 80s, 90s: learning ranking algorithms based on user feedback
  - 2000s: text categorization
- Limited by amount of training data
- Web query logs have generated new wave of research
  - e.g., "Learning to Rank"

### Generative vs. Discriminative

- All of the probabilistic retrieval models presented so far fall into the category of generative models
  - A generative model assumes that documents were generated from some underlying model (in this case, usually a multinomial distribution) and uses training data to estimate the parameters of the model
  - probability of belonging to a class (i.e. the relevant documents for a query) is then estimated using Bayes' Rule and the document model

### Generative vs. Discriminative

- A discriminative model estimates the probability of belonging to a class directly from the observed features of the document based on the training data
- Generative models perform well with low numbers of training examples
- Discriminative models usually have the advantage given enough training data
  - Can also easily incorporate many features

### Discriminative Models for IR

- Discriminative models can be trained using explicit relevance judgments or click data in query logs
- Large class of algorithms called *learning to*
  - Learns weights on a linear (or non-linear)
     combination of features that is used to rank documents
  - Best weights optimize a performance metric

Training data is

$$(q_1, r_1), (q_2, r_2), \ldots, (q_n, r_n)$$

- r is partial rank information
  - if document  $d_a$  should be ranked higher than  $d_b$ , then  $(d_a, d_b) \subseteq r_i$
- partial rank information comes from relevance judgments (allows multiple levels of relevance) or click data
  - e.g., d₁, d₂ and d₃ are the documents in the first, second and third rank of the search output, only d₃ clicked on → (d₃, d₁) and (d₃, d₂) will be in desired ranking for this query

- Learning a linear ranking function  $\vec{w}.\vec{d_a}$ 
  - where w is a weight vector that is adjusted by learning
  - $-d_a$  is the vector representation of the features of document
  - non-linear functions also possible
- Weights represent importance of features
  - learned using training data
  - e.g.,  $\vec{w}.\vec{d} = (2,1,2).(2,4,1) = 2.2 + 1.4 + 2.1 = 10$

 Learn w that satisfies as many of the following conditions as possible:

$$\forall (d_i, d_j) \in r_1 : \vec{w}.\vec{d_i} > \vec{w}.\vec{d_j}$$

$$\cdots$$

$$\forall (d_i, d_j) \in r_n : \vec{w}.\vec{d_i} > \vec{w}.\vec{d_j}$$

Can be formulated as an optimization problem

$$\begin{array}{ll} minimize: & \frac{1}{2}\vec{w}.\vec{w} + C\sum \xi_{i,j,k} \\ subject\ to: \\ \forall (d_i,d_j) \in r_1 : \vec{w}.\vec{d_i} > \vec{w}.\vec{d_j} + 1 - \xi_{i,j,1} \\ & \cdots \\ \forall (d_i,d_j) \in r_n : \vec{w}.\vec{d_i} > \vec{w}.\vec{d_j} + 1 - \xi_{i,j,n} \\ \forall i \forall j \forall k: \xi_i, j, k \geq 0 \end{array}$$

 $-\xi$ , known as a slack variable, allows for misclassification of difficult or noisy training examples, and C is a parameter that is used to prevent overfitting

- Software available to do optimization
- Each pair of documents in our training data can be represented by the vector:

$$(\vec{d_i} - \vec{d_j})$$

Score for this pair is:

$$\vec{w}.(\vec{d_i} - \vec{d_j})$$

- SVM classifier will find a w that makes the smallest score as large as possible
  - make the differences in scores as large as possible for the pairs of documents that are hardest to rank

## **Topic Models**

- Improved representations of documents
  - can also be viewed as improved smoothing techniques
  - improve estimates for words that are related to the topic(s) of the document
    - instead of just using background probabilities
- Approaches
  - Heuristic
    - Latent Semantic Indexing (LSI)
  - Probabilistic and Generative
    - Probabilistic Latent Semantic Indexing (pLSI)
    - Latent Dirichlet Allocation (LDA)

### Text Reuse

#### Jobless rate at 3-year low as payrolls surge



Recommend I 1,328 people recommend this.



By Lucia Mutikani WASHINGTON | Fri Feb 3, 2012 5:35pm EST

(Reuters) - The United States created jobs at the fastest pace in nine months in January and the unemployment rate unexpectedly dropped to a near three-year low, giving a boost to President Barack Obama.



TrimTabs

### REUTERS By Lucia Mutikani | Reuters – 4 hrs ago Recommend < 81 RELATED CONTENT Job seekers stand in line to speak with an employer at a job fair in San Francisco, ... Article: Instant view: January nonfarm payrolls rose by 15 hrs ago Article: Snap analysis: Job creation accelerates broadly 15 hrs ago POLITICS SLIDESHOWS

Manning faces

#### Jobless rate at 3-year low as payrolls surge

WASHINGTON (Reuters) - The United States created jobs at the fastest pace in nine months in January and the unemployment rate unexpectedly dropped to a near three-year low, giving a boost to President Barack Obama.

Nonfarm payrolls jumped 243,000, the Labor Department said on Friday, as factory jobs grew by the most in a year. The jobless rate fell to 8.3 percent - the lowest since February 2009 - from 8.5 percent in December.

The gain in employment was the largest since April and it far outstripped the 150,000 predicted in a Reuters poll of economists. It hinted at underlying economic strength and lessened chances of further stimulus from the Federal Reserve.

"More pistons in the economic engine have begun to fire, pointing to accelerating economic growth. One of the happiest persons reading this job report is President Obama," said Sung Won Sohn, an economics professor at California State University Channel Islands.

The payroll gains were widespread - from retail to temporary help, and from construction to manufacturing - an indication the recovery was becoming more durable.

### **Topical Similarity**

#### Job Gains Reflect Hope a Recovery Is Blooming



A job applicant received assistance at an employment fair in Modesto, Calif., this week.

By MOTOKO RICH

Published: February 3, 2012

The front wheels have lifted off the runway. Now, Americans are waiting to see if the economy can truly get aloft.



With the government reporting that the unemployment rate and the number of jobless fell in January to the lowest levels since early 2009, the recovery seems finally to be reaching American workers.

The Labor Department's latest



#### Jobless rate at 3-year low as payrolls surge

REUTERS By Lucia Mutikani | Reuters – 4 hrs ago

Recommend < 81



Manning faces

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### Parallel Bitext

Genehmigung des Protokolls
Das Protokoll der Sitzung vom
Donnerstag, den 28. März 1996
wurde verteilt.
Gibt es Einwände?
Die Punkte 3 und 4 widersprechen
sich jetzt, obwohl es bei der
Abstimmung anders aussah.
Das muß ich erst einmal klären,
Frau Oomen-Ruijten.

Approval of the minutes
The minutes of the sitting of
Thursday, 28 March 1996 have
been distributed.
Are there any comments?
Points 3 and 4 now contradict one
another whereas the voting
showed otherwise.
I will have to look into that, Mrs
Oomen-Ruijten.

Koehn (2005): European Parliament corpus

## Multilingual Topical Similarity

#### Abraham Lincoln

From Wikipedia, the free encyclopedia

This article is about the American president. For other uses, see Abraham Lincoln (disambiguation).

Abraham Lincoln | Injken/ (February 12, 1809 – April 15, 1865) was the legislator, and a one-term member of the United States House of Representatives, but failed in two attempts to be elected to the United States Senate.

#### Abraham Lincoln

Abraham Lincoln ['exbrehæm 'linken] (\* 12. Februar 1809 bei Hodgenville, Hardin County, heute: LaRue County, Kentucky; † 15. April 1865 in Washington, D.C.) amtierte von 1861 bis 1865 als 16. Präsident der Vereinigten Staaten von Amerika. Er war der erste aus den Reihen der Republikanischen Partei und der erste, der einem Attentat zum Opfer fiel. 1860 gewählt, gelang ihm 1864 die Wiederwahl.

Seine Präsidentschaft gilt als eine der bedeutendsten in der Geschichte der Vereinigten Staaten: Die Wahl des Sklavereigegners veranlasste zunächst sieben, später weitere vier der sklavenhaltenden Südstaaten zur Sezession. Lincoln führte die verbliebenen Nordstaaten durch den daraus entstandenen Bürgerkrieg, setzte die Wiederherstellung der Union durch und betrieb erfolgreich die Abschaffung der Sklaverei in den Vereinigten Staaten. Unter seiner Regierung schlugen die USA den Weg zum zentral regierten, modernen Industriestaat ein und schufen so die Basis für ihren Aufstieg zur Weltmacht im 20. Jahrhundert.

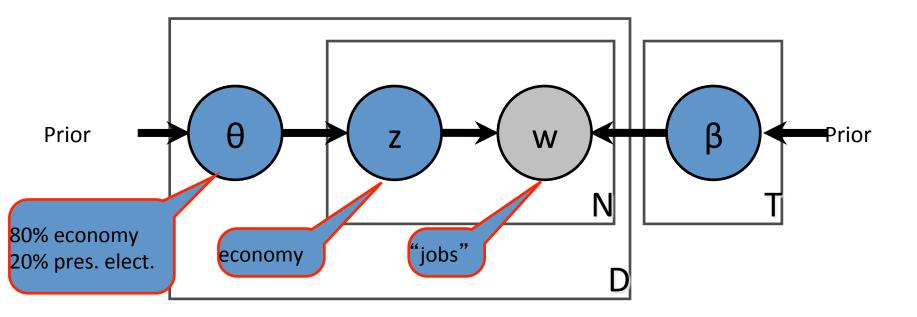
### What Representation?

- Bag of words, n-grams, etc.?
  - Vocabulary mismatch within language:
    - Jobless vs. unemployed
  - What about between languages?
    - Translate everything into English?
- Represent documents/passages as probability distributions over hidden "topics"

## Modeling Text with Topics

Latent Dirichlet Allocation (Blei, Ng, Jordan 2003)

- Let the text talk about T topics
- Each topic is a probability dist'n over all words
- For D documents each with N<sub>D</sub> words:



# Top Words by Topic

*Topics*  $\rightarrow$ 

1	2	3	4	5	6	7	8
DISEASE	WATER	MIND	STORY	FIELD	SCIENCE	BALL	JOB
BACTERIA	FISH	WORLD	STORIES	MAGNETIC	STUDY	GAME	WORK
DISEASES	SEA	DREAM	TELL	MAGNET	SCIENTISTS	TEAM	JOBS
GERMS	SWIM	DREAMS	CHARACTER	WIRE	SCIENTIFIC	FOOTBALL	CAREER
FEVER	SWIMMING	THOUGHT	CHARACTERS	NEEDLE	KNOWLEDGE	BASEBALL	EXPERIENCE
CAUSE	POOL	IMAGINATION	AUTHOR	CURRENT	WORK	PLAYERS	EMPLOYMENT
CAUSED	LIKE	MOMENT	READ	COIL	RESEARCH	PLAY	OPPORTUNITIES
SPREAD	SHELL	THOUGHTS	TOLD	POLES	CHEMISTRY	FIELD	WORKING
VIRUSES	SHARK	OWN	SETTING	IRON	TECHNOLOGY	PLAYER	TRAINING
INFECTION	TANK	REAL	TALES	COMPASS	MANY I	BASKETBALL	
VIRUS	SHELLS	LIFE	PLOT	LINES	MATHEMATICS		CAREERS
MICROORGANISMS		IMAGINE	TELLING	CORE	BIOLOGY	PLAYED	POSITIONS
PERSON	DIVING	SENSE	SHORT	ELECTRIC	FIELD	PLAYING	FIND
INFECTIOUS	DOLPHINS	CONSCIOUSNES	S FICTION	DIRECTION	PHYSICS	HIT	POSITION
COMMON	SWAM	STRANGE	ACTION	FORCE	LABORATORY	TENNIS	FIELD
CAUSING	LONG	FEELING	TRUE	MAGNETS	STUDIES	TEAMS	OCCUPATIONS
SMALLPOX	SEAL	WHOLE	EVENTS	BE	WORLD	GAMES	REQUIRE
BODY	DIVE	BEING	TELLS	MAGNETISM		SPORTS	OPPORTUNITY
INFECTIONS	DOLPHIN	MIGHT	TALE	POLE	STUDYING	BAT	EARN
CERTAIN	UNDERWATER	HOPE	NOVEL	INDUCED	SCIENCES	TERRY	ABLE

Griffiths et al.

# Top Words by Topic

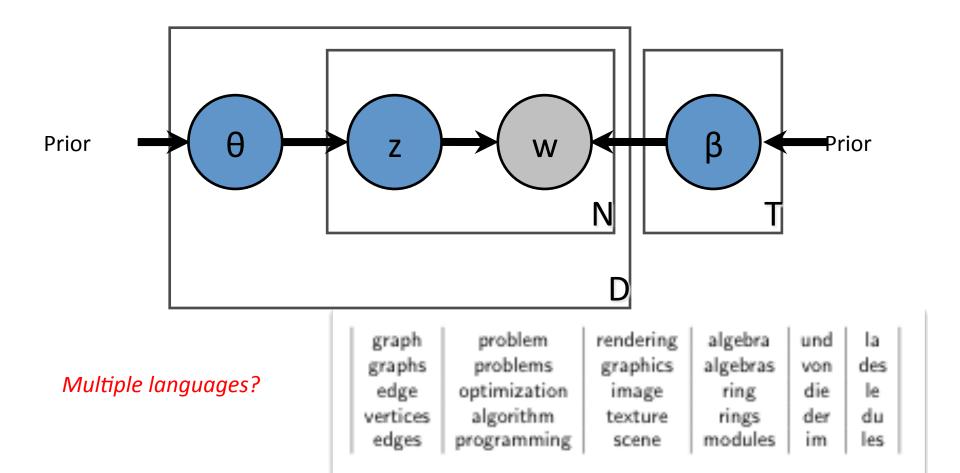
*Topics*  $\rightarrow$ 

1	2	3	4	5	6	7	8
DISEASE	WATER	MIND	STORY	FIELD	SCIENCE	BALL	JOB
BACTERIA	FISH	WORLD	STORIES	MAGNETIC	STUDY	GAME	WORK
DISEASES	SEA	DREAM	TELL	MAGNET	SCIENTISTS	TEAM	JOBS
GERMS	SWIM	DREAMS	CHARACTER	WIRE	SCIENTIFIC	FOOTBALL	CAREER
FEVER	SWIMMING	THOUGHT	CHARACTERS	NEEDLE	KNOWLEDGE	BASEBALL	EXPERIENCE
CAUSE	POOL	IMAGINATION	AUTHOR	CURRENT	WORK	PLAYERS	EMPLOYMENT
CAUSED	LIKE	MOMENT	READ	COIL	RESEARCH	PLAY	OPPORTUNITIES
SPREAD	SHELL	THOUGHTS	TOLD	POLES	CHEMISTRY	FIELD	WORKING
VIRUSES	SHARK	OWN	SETTING	IRON	TECHNOLOGY	PLAYER	TRAINING
INFECTION	TANK	REAL	TALES	COMPASS	MANY I	BASKETBALI	
VIRUS	SHELLS	LIFE	PLOT	LINES	MATHEMATICS	COACH	CAREERS
MICROORGANISMS		IMAGINE	TELLING	CORE	BIOLOGY	PLAYED	POSITIONS
PERSON	DIVING	SENSE	SHORT	ELECTRIC	FIELD	PLAYING	FIND
INFECTIOUS	DOLPHINS	CONSCIOUSNESS	S FICTION	DIRECTION	PHYSICS	HIT	POSITION
COMMON	SWAM	STRANGE	ACTION	FORCE	LABORATORY	TENNIS	FIELD
CAUSING	LONG	FEELING	TRUE	MAGNETS	STUDIES	TEAMS	OCCUPATIONS
SMALLPOX	SEAL	WHOLE	EVENTS	BE	WORLD	GAMES	REQUIRE
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CERTAIN	UNDERWATER	HOPE	NOVEL	INDUCED	SCIENCES	TERRY	ABLE

Griffiths et al.

### **Modeling Text with Topics**

Latent Dirichlet Allocation (Blei, Ng, Jordan 2003)



### LDA

- Model document as being generated from a mixture of topics
  - 1. For each document D, pick a multinomial distribution  $\theta_D$  from a Dirichlet distribution with parameter  $\alpha$ ,
  - 2. For each word position in document D,
    - (a) pick a topic z from the multinomial distribution  $\theta_D$ ,
    - (b) Choose a word w from  $P(w|z,\beta)$ , a multinomial probability conditioned on the topic z with parameter  $\beta$ .

### LDA

Gives language model probabilities

$$P_{lda}(w|D) = P(w|\theta_D, \beta) = \sum_{z} P(w|z, \beta)P(z|\theta_D)$$

 Used to smooth the document representation by mixing them with the query likelihood probability as follows:

$$P(w|D) = \lambda \left( \frac{f_{w,D} + \mu \frac{c_w}{|C|}}{|D| + \mu} \right) + (1 - \lambda) P_{lda}(w|D)$$

### LDA

- If the LDA probabilities are used directly as the document representation, the effectiveness will be significantly reduced because the features are too smoothed
  - e.g., in typical TREC experiment, only 400 topics used for the *entire* collection
  - generating LDA topics is expensive
- When used for smoothing, effectiveness is improved

## LDA Example

### Top words from 4 LDA topics from TREC news

Arts	Budgets	Children	Education
new	million	children	school
$\operatorname{film}$	ax	women	students
show	program	people	schools
music	budget	$\operatorname{child}$	education
movie	billion	years	teachers
play	federal	families	high
musical	year	work	public
best	spending	parents	teacher
actor	new	says	bennett
$\operatorname{first}$	state	family	manigat
york	plan	welfare	namphy
opera	money	men	state
theater	programs	percent	president
actress	government	care	elementary
love	congress	life	haiti

### Summary

- Best retrieval model depends on application and data available
- Evaluation corpus (or test collection), training data, and user data are all critical resources
- Open source search engines can be used to find effective ranking algorithms
  - Galago query language makes this particularly easy
- Language resources (e.g., thesaurus) can make a big difference