

Copyright (c) 2017, Gene Cooperman. May be freely distributed and modified as long as this copyright notice remains.

For ABA problem, see: https://en.wikipedia.org/wiki/ABA_problem

NOTE: The label “*pop2a*” in *popStack()* below “causes” the bug to be exposed. Try deleting it. This would have the effect of atomically executing:

```
CAS(HEAD, local_myhead, address[local_myhead].next);
```

because it hides the internal assembly code that first computes the register value, *reg_next*, and then executes *CAS()*.

Note that the field “*onStack*” is present only for debugging, and for assertions. Don’t hesitate to add extra fields and variables to ease the job of model checking.

The bug is the ABA problem. When illustrating this bug, the errors in the “Model Checking Results” tab will have too many frames to easily read. You can then remove many of the unnecessary labels in other routines to easily see the cause of the bug: the ABA problem.

Always include these *PlusCal* modules for basic data types.

EXTENDS *Naturals*, *Sequences*, *TLC*, *FiniteSets*

These constants will have to be assigned a value within the generated module.

CONSTANTS *MAX_ITER*, *MAX_STACK_SIZE*

NUM_THREADS is a PRE-DEFINED constant. It cannot be changed later.

NUM_THREADS \triangleq 2

null is a unique value (pre-defined constant)

NULL \triangleq CHOOSE *n* : *n* \notin 1 .. *MAX_STACK_SIZE*

--algorithm *LockFreeStack*{

variables *retVal* = [*thread* \in 1 .. *NUM_THREADS* \mapsto *NULL*],
address = [*addr* \in 1 .. *MAX_STACK_SIZE* \mapsto
[*next* \mapsto *NULL*, *onStack* \mapsto FALSE, *data* \mapsto 0]],
initialized = FALSE;
HEAD;

CAS: compare-and-swap

CAS must be a macro. This reflects that it is an assembly instruction

that modifies its arguments. It must not use the call-by-value of a procedure.

CAS is atomic. So, there are no intermediate labels.

macro *CAS*(*x*, *y*, *z*)

```
{
  if ( x = y ) {
    x := z; swap y for z as value of x
    retVal[self] := TRUE;
  } else {
    retVal[self] := FALSE;
  }
}
```

```

    } ;
  }

procedure pushStack( elt )
  variable local_myhead ;
{
  push1: address[elt].next := HEAD ;
  push2: assert address[elt].onStack = FALSE ;
  push3: address[elt].onStack := TRUE ;
  tryAgainPush: local_myhead := HEAD ;
    push5a: address[elt].next := local_myhead ;
    push5b: CAS(HEAD, local_myhead, elt) ;
    push5c: if (  $\neg$ retVal[self] ) {
    push5d: goto tryAgainPush ;
    } ;
  endPush: return ;
}

procedure popStack( )
  variable local_myhead, reg_next, elt ;
{
  tryAgainPop:
    local_myhead := HEAD ;
  pop1: if ( local_myhead = 0 ) { // If I believe HEAD = 0, return now.
  pop1a: retVal[self] := NULL ;
  pop1b: return ;
    } ;

  pop2: reg_next := address[local_myhead].next ;
  pop2a: CAS(HEAD, local_myhead, reg_next) ;
  pop2b: if (  $\neg$ retVal[self] ) {
  pop2c: goto tryAgainPop ;
    } ;

  pop3: elt := local_myhead ;
  pop4: assert address[elt].onStack = TRUE ;
  pop5: address[elt].onStack := FALSE ;
  endPop: retVal[self] := elt ;
  return ;
}

process ( thread  $\in$  1 .. NUM_THREADS )
  variable my_set = {}, myelt,
    init_thread, iterations = MAX_ITER ;
{
  init1: init_thread := CHOOSE thr  $\in$  1 .. NUM_THREADS : TRUE ;
  init2: if ( self = init_thread ) { // This thread will initialize global data

```

```

init4: HEAD := 0;
init5: while ( HEAD < MAX_STACK_SIZE ) {
init6:   address[HEAD + 1] := [next ↦ HEAD, onStack ↦ TRUE, data ↦ 1];
init7:   HEAD := HEAD + 1;
        };
init8:   initialized := TRUE; //init_thread will set this global var
        };
init9: await initialized; // all threads will wait for this

th1: while ( iterations > 0 ) {
th2:   either { if ( my_set ≠ {} ) {
        // Set myelt at random (non-deterministically)
th2a:     with ( tmp ∈ my_set ) { myelt := tmp } ;
th2b:     my_set := my_set \ {myelt};
th2c:     call pushStack(myelt);
        } }
        or {
th3a:     call popStack();
th3b:     if ( retVal[self] ≠ NULL ) {
th3c:     my_set := my_set ∪ {retVal[self]} Add the popped elt to my_set
        } } ;
th4: iterations := iterations - 1;
    } ; end while
} ; end process

} \* end algorithm

```

```

\* Modification History
\* Last modified Thu Apr 11 13:35:54 EDT 2019 by gene
\* Last modified Sun Oct 22 06:26:25 EDT 2017 by celestekostopulos-cooperman
\* Created Fri Oct 20 22:08:53 EDT 2017 by celestekostopulos-cooperman

```